

## Chapter 3 Functions

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### Section 3.1 Defining Functions

#### Video 1:

Is the relation a function? If so, state the domain and range:

a)  $\{(-3,5),(-3,2),(0,3),(1,7)\}$

b)  $\{(-2,0),(1,8),(2,0),(5,3)\}$

#### Video 2:

Does the equation define  $y$  as a function of  $x$ ?

a)  $x + y^2 = 2$

b)  $y = \frac{3x-1}{x+2}$

c)  $y = x^2 + 1$

#### Video 3:

For the function, find  $f(0)$ ,  $f(-x)$ , and  $f(x+h)$ :

a)  $f(x) = \frac{2x+3}{3x-1}$

#### Video 4:

Find the domain of each function:

a)  $f(x) = x^2 + 3$

b)  $g(x) = \frac{x}{x^2 - 9}$

c)  $h(x) = \frac{2}{\sqrt{x-5}}$

d)  $g(w) = \frac{\sqrt{w+7}}{w-3}$

Video 5:

For the pair of functions, find  $(f-g)(x)$  and  $(fg)(2)$ :

$$f(x) = 3x + 4 ; g(x) = 2x - 5$$

Video 6:

For the pair of functions, find  $(f/g)(1)$  and  $(fg)(x)$ :

$$f(x) = \sqrt{x+2} ; g(x) = \frac{1}{x}$$

Video 7:

Find the difference quotient  $\frac{f(x+h) - f(x)}{h}$

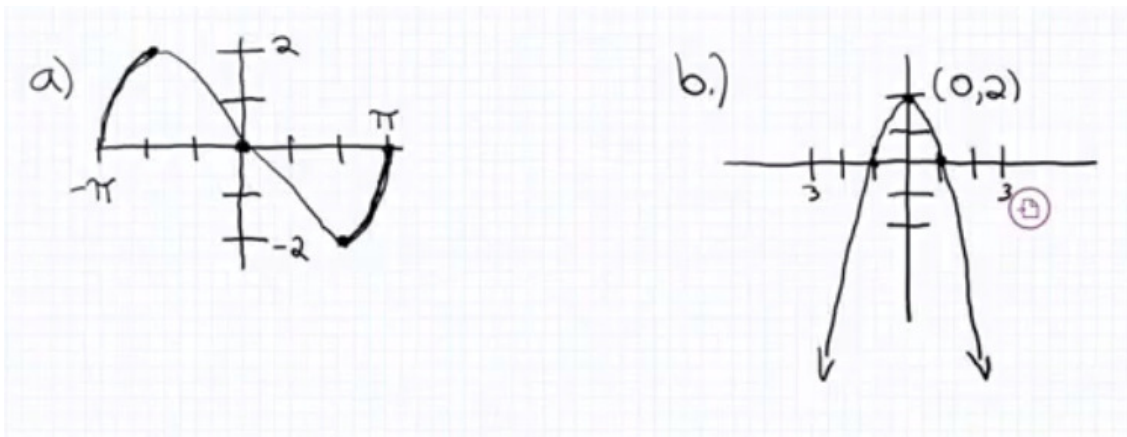
a)  $f(x) = x^2 - 3x + 1$

b)  $f(x) = \sqrt{x+2}$

### Section 3.2 Graphing Functions

Video 1:

Is the graph that of a function? If so, state the domain, range, intercepts, and symmetry



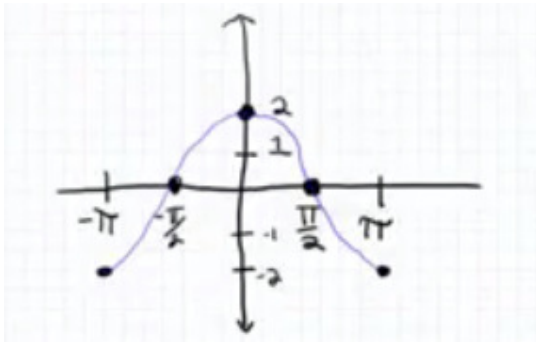
Video 2: Use the function below to answer the following questions  $f(x) = \frac{x^2 + 1}{x + 4}$

- Is  $(1, \frac{2}{5})$  on the graph?
- If  $x = 0$ , what is  $f(x)$ ?
- If  $f(x) = \frac{1}{2}$ , what is  $x$ ?
- What is the domain of  $f(x)$ ?
- List the  $x$  intercepts
- List the  $y$  intercepts

### Section 3.3 Properties of Functions

Video 1:

Use the graph of function below to find the following



- Intercepts
- Domain and range
- Intervals on which the graph increases, decreases, or is constant
- Whether it is even, odd, or neither

Video 2:

Determine if the function is even, odd, or neither  $f(x) = -2x + |x|$

Video 3:

Determine if the function is even, odd, or neither:

- $f(x) = 3x^4 - x^2$
- $h(x) = \frac{-x^5}{3x^2 - 7}$
- $g(x) = 3x^3 + 2$

Video 4:

Find the average rate of change:  $\frac{\Delta y}{\Delta x} = \frac{f(b) - f(a)}{b - a}$

$$g(x) = x^2 - 2x + 1$$

a) From -1 to 1

b) From 0 to 3

c) From 3 to 4

### Section 3.4 A Library of Functions

Video 1:

Graph the following functions:  $h(x) = 5$ ,  $g(x) = x$ ,  $f(x) = x^2$ ,  $h(x) = x^3$ ,  $g(x) = \sqrt{x}$ ,  $f(x) = |x|$ ,

$$g(x) = \frac{1}{x}$$

Video 2:

Find the following:  $f(-3)$ ,  $f(0)$ ,  $f(2)$

$$f(x) = \begin{cases} -2x & x < 0 \\ 1 & x = 0 \\ 2x^2 - 1 & x > 0 \end{cases}$$

Video 3:

Graph the following and find the domain and range:

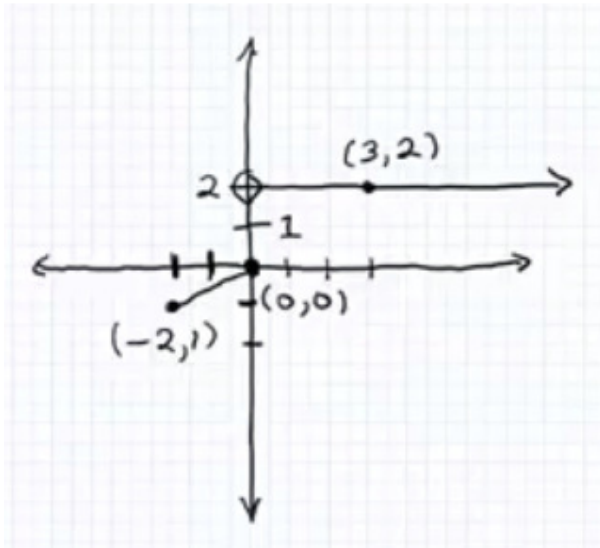
$$f(x) = \begin{cases} 2 - x \\ \sqrt{x} \end{cases}$$

If  $-4 \leq x < 1$

If  $x > 1$

Video 4:

Write a definition for the function that is graphed below:



### Section 3.5 Graphing Transformations

Video 1:

Graph the following:  $y = x^2$ ,  $y = x^2 + 3$ ,  $y = (x-3)^2$ ,  $y = -x^2 + 3$ ,  $y = -(x+2)^2$ ,  $y = 2x^2$ ,  
 $y = (2x)^2$

Video 2:

Write a function whose graph is  $y = |x|$  but is:

- Shifted to do the right 4 units
- Shifted down 4 units
- Reflected across the x axis
- Vertically stretched by a factor of 4
- Horizontally stretched by a factor of 4

Video 3:

If the x-intercepts of  $y = f(x)$  are -7 and 1:

- What are the x-intercepts of  $y = f(x+4)$
- What are the x-intercepts of  $y = f(x-3)$
- What are the x-intercepts of  $y = 2f(x)$
- What are the x-intercepts of  $y = f(-x)$

Video 4:

Graph the following functions

a)  $f(x) = 3(x-1)^2 + 2$

b)  $f(x) = \sqrt{-x} - 3$

Section 3.6 Crating Functions

Video 1:

Let  $P = (x, y)$  be a point on the graph of:  $y = -x^2 - 4$

- a) Express the distance  $d$  from  $P$  to the point  $(0, -2)$  as a function of  $x$
- b) What is  $d$  if  $x = -2$

Video 2:

Let  $P = (x, y)$  be a point on the graph of:  $x^2 + y^2 = 9$